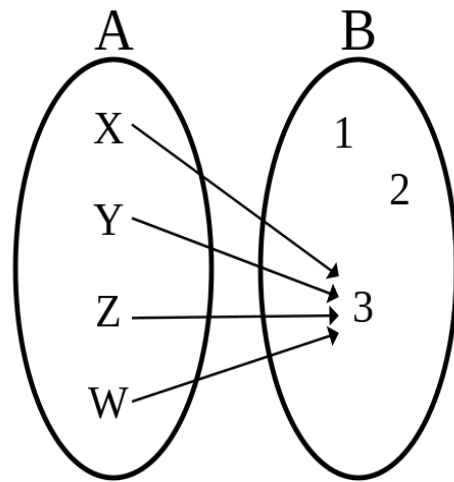
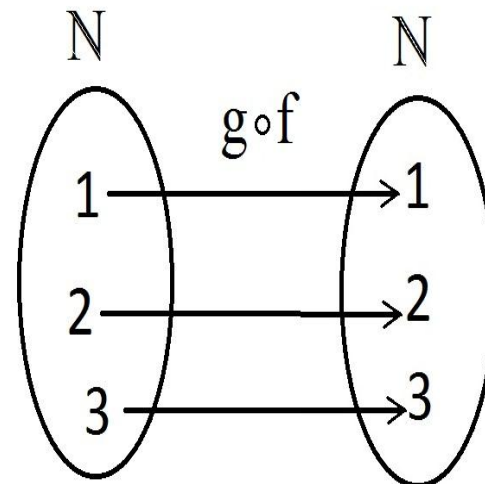


## Functions:

- ▶ Constant function
- ▶ Identity function
- ▶ Trigonometric function
- ▶ Composite function
- ▶ Inverse function



Constant function



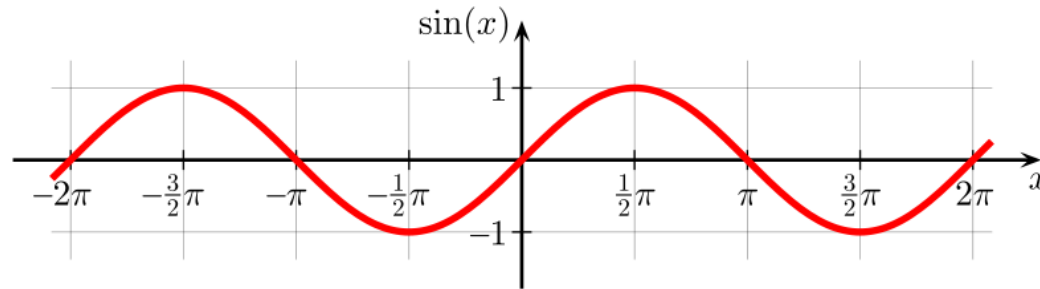
Identity function

## Trigonometric function

- ▶ The function taking trigonometric ratio as an independent variable is called trigonometric function.

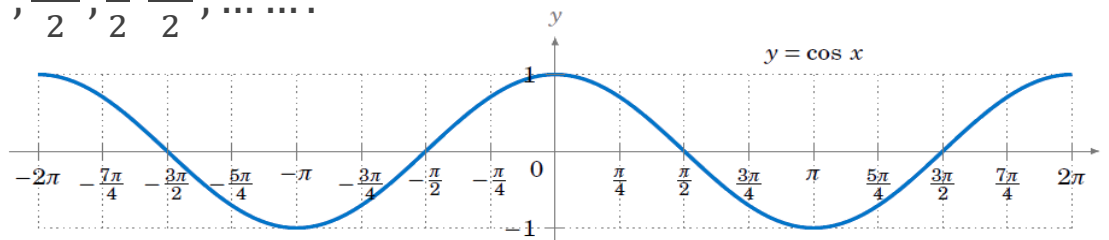
### Sine functions:

- The y-intercept of  $\sin x$  is 0.
- The x-intercepts are  $\dots -2\pi, -\pi, 0, \pi, 2\pi, \dots$
- The domain is  $(-\infty, +\infty)$ .
- The range is  $[-1, 1]$ .



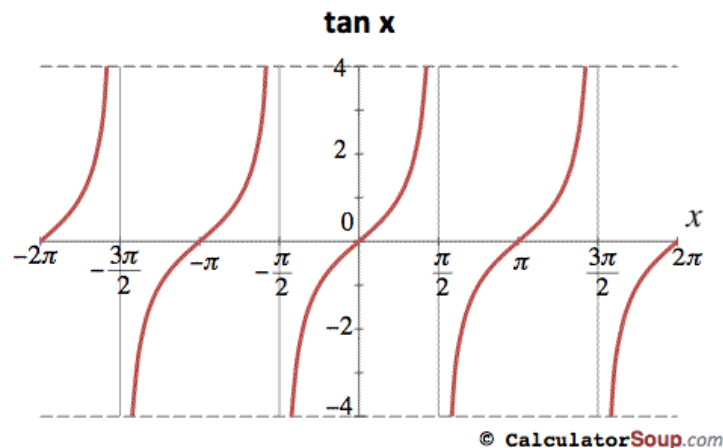
## Cosine functions:

- The y-intercept is 1.
- The x - intercepts are  $\dots, -\frac{3\pi}{2}, -\frac{\pi}{2}, \frac{\pi}{2}, \frac{3\pi}{2}, \dots$
- The domain is  $(-\infty, +\infty)$ .
- The range is  $[-1, 1]$ .



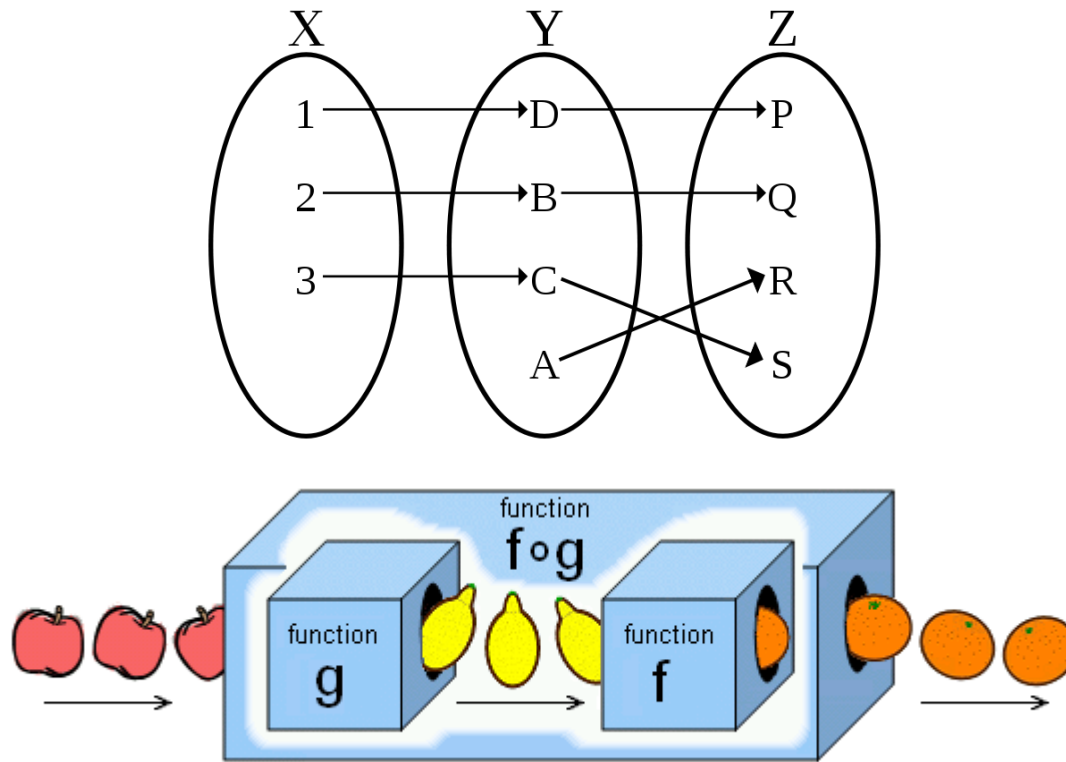
## Tangent functions:

- The y-intercept is 0.
- The x-intercepts are  $\dots, -2\pi, -\pi, 0, \pi, 2\pi, \dots$
- The domain is  $(-\infty, +\infty)$  excluding  $\frac{\pi}{2} + n\pi$ .
- The range is  $(-\infty, +\infty)$ .



## Composite function

- Let  $g:X \rightarrow Y$  and  $f:Y \rightarrow Z$  are two functions. A function from  $X$  to  $Z$  is called composite function if it maps every element of  $X$  to unique elements of  $Z$ .



## Composite function

### Worked Out Example: 1

- If  $f(x) = 3x + 4$  and  $g(x) = 2x - 5$ , find  $f \circ g(x)$  and  $g \circ f(x)$ .

Solution:  $f(x) = 3x + 4$  and  $g(x) = 2x - 5$

$$\begin{aligned}f \circ g(x) &= f(g(x)) \\ &= f(2x - 5) \\ &= 3(2x - 5) + 4 \\ &= 6x - 15 + 4 \\ &= 6x - 11\end{aligned}$$

$$\begin{aligned}g \circ f(x) &= g(f(x)) \\ &= g(3x + 4) \\ &= 2(3x + 4) - 5 \\ &= 6x + 8 - 5 \\ &= 6x + 3\end{aligned}$$

Hence,  $f \circ g(x) \neq g \circ f(x)$

## Worked Out Example: 2

- ▶  $f(x) = 2x + 3$  and  $f(g(x)) = 4x + 5$ , find  $g(x)$ .

Hint: Start from  $f(x)$ .

$$f(x) = 2x + 3,$$

or,  $f(g(x)) = 2g(x) + 3,$

or,  $4x + 5 = 2g(x) + 3,$

on simplifying,  $g(x) = 2x + 1$

- ▶ If  $g(x) = 3x - 4$  and  $f(g(x)) = 6x + 5$ , find  $f(x)$ .

Hint: start from  $f(g(x))$ .

$$f(g(x)) = 6x + 5$$

or,  $f(g(x)) = 6x + 5$

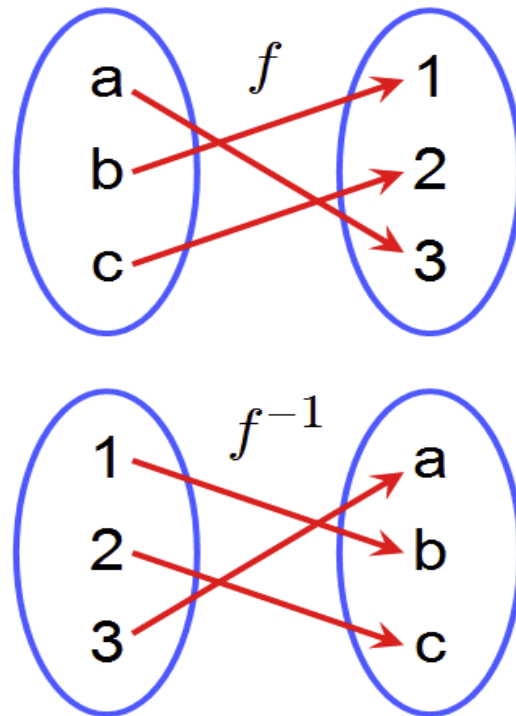
or,  $f(3x - 4) = 6x + 5$

or,  $f(3x - 4) = 2(3x - 4) + 5 + 8$

or,  $f(x) = 2x + 13$

## Inverse function

- ▶ Let  $f:A \rightarrow B$  be an one-to-one onto function. A new function from  $B$  to  $A$  is the inverse function of the given function.



## Inverse function

### Worked Out Example: 1

- Find the inverse of the function  $f(x) = 3x + 5$ .

Solution:

$$\text{Let } y = f(x) = 3x + 5$$

$$\text{or, } y = 3x + 5$$

Interchanging  $x$  and  $y$ , we get,

$$x = 3y + 5$$

Solve to get the value of  $y$

$$\text{or, } x - 5 = 3y$$

$$\text{or, } 3y = x - 5$$

$$\text{or, } y = \frac{x - 5}{3}$$

This is the inverse of the given function.



## Worked Out Example: 2

- ▶ Find the inverse of  $f(x) = \frac{2x+3}{5x-4}$
- ▶ let  $y = f(x) = \frac{2x+3}{5x-4}$
- ▶  $y = \frac{2x+3}{5x-4}$
- ▶ Interchanging the values of  $x$  and  $y$ .
- ▶  $x = \frac{2y+3}{5y-4}$
- ▶ Solve in such a way that only one  $y$  is there and keep in LHS.
- ▶  $5xy - 4x = 2y + 3$
- ▶  $5xy - 2y = 4x + 3$
- ▶  $y(5x - 2) = 4x + 3$
- ▶ So,  $y = f^{-1}(x) = \frac{4x+3}{5x-2}$
- ▶ Hence the inverse of  $\frac{ax+b}{cx+d}$  is  $\frac{-dx+b}{cx-a}$

## Exercise:

- 1) Define trigonometric function.
- 2) What is the y-intercept of  $y = \sin x$ ?
- 3) Write the domain of  $y = \tan x$ .
- 4) What is the range of  $y = \cos x$ ?
- 5) Define composite function with example.
- 6) If  $f(x) = 2x + 7$  and  $g(x) = 5x - 3$ , find  $f \circ g(x)$  and  $g \circ f(x)$ .
- 7) If  $f(x) = 3x - 4$  and  $g(x) = x^2$ , find  $f \circ g(x)$  and  $g \circ f(x)$ .
- 8) If  $f(x) = 2x - 5$  and  $f \circ g(x) = 8x + 5$ , find  $g(x)$ .
- 9) If  $g(x) = 3x - 2$  and  $f \circ g(x) = 6x + 4$ , find  $f(x)$ .
- 10) Define inverse function.
- 11) Find the inverse of the given functions:
  - a)  $f(x) = 2x + 7$
  - b)  $f(x) = 7x - 3$
  - c)  $f(x) = \frac{3x - 5}{4x + 2}$
  - d)  $g(x) = \frac{5x - 3}{2x + 7}$

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